

1. (a) There is no asymmetry of information. **(+10 pts)**
 (b) Outcome could be inefficient as there are cases when trade opportunities are not exploited. **(+10 pts)**

(c) Expected profit of B: $E(\pi) = (p - c) * (1 - F(p))$

Answer: $p = \frac{c + \bar{v}}{2}$ **(+8 pts)**

2. (a) Various answers. **(+5 pts)**

(b) There is hidden action, which indicates the presence of moral hazard. **(+5 pts)**

(c) IC: *Expected Utility (cheating) ≥ Expected Utility (no cheating)* **(+5 pts)**

IC: $(1 - p) * (Utility(grade = 40) * 0,5 + Utility(grade = 60) * 0,5) \geq Utility(grade = 40) * 0,25 + Utility(grade = 60) * 0,25$ **(+3 pts)**

so, $p \leq \frac{1}{2}$ **(+2 pts)**

(d) Assume penalty for cheating is some x that tends to minus infinity, so utility of x is negative

IC becomes:

$$p \leq \frac{EU(\text{no cheating})}{EU(\text{cheating successfully}) - Utility(x)} \quad \textbf{(+3 pts)}$$

As in this case $Utility(x)$ approaches minus infinity, p is equal to zero. So, high enough penalty successfully discourages cheating. **(+2 pts)**

3. (a) Yes, as probability of success with high effort is higher than probability of success with low effort (50% vs. 40%). **(+10 pts)**

(b) Effort is unobservable, so the residual claimant (RC) has two options:

$E = 0$: $w = 16$ (reservation wage); $E\Pi = 0,4\Pi_H + 0,6\Pi_L - 16$ **(+3 pts)**

$E = 1$: Make up such a contract that manager exerts full effort and RC maximizes expected net profit:

$$\max_{w_h, w_l} 0,5 * (\Pi_H - w_H) + 0,5 * (\Pi_L - w_L)$$

s.t.

$$\text{IR: } 0,5 * \left(w_h^{\frac{1}{2}} - 1 \right) + 0,5 * \left(w_L^{\frac{1}{2}} - 1 \right) \geq 4$$

$$\text{IC: } 0,5 * \left(w_h^{\frac{1}{2}} - 1 \right) + 0,5 * \left(w_L^{\frac{1}{2}} - 1 \right) \geq 0,4 * \left(w_h^{\frac{1}{2}} \right) + 0,6 * \left(w_L^{\frac{1}{2}} \right)$$

That yields: $w_L = 0, w_H = 100$ and $E(\text{net profit}) = 0,5 * \Pi_H + 0,5 * \Pi_L - 50$ **(+7 pts)**

$E = 1$ is preferred to $E = 0$ if $E(\text{net profit} | \text{high effort}) \geq E(\text{net profit} | \text{low effort})$, what is equivalent to $\Pi_H - \Pi_L \geq 340$ **(+2 pts)**

So, optimal contract is:

$$w = \begin{cases} w_0 = 16, & \text{if } \Pi_H - \Pi_L < 340 \\ \begin{cases} w_H = 100 \\ w_L = 0 \end{cases} & \text{if } \Pi_H - \Pi_L \geq 340 \end{cases} \quad (+3 \text{ pts})$$

(c) If information is observable contract will be contingent on effort:

$$e = 0: w_0 = 16, E(\text{net profit}) = 0,4 * \Pi_H + 0,6 * \Pi_L - 16 \quad (+2 \text{ pts})$$

$$e = 1: w = 25, E(\text{net profit}) = 0,5 * \Pi_H + 0,5 * \Pi_L - 25 \quad (+3 \text{ pts})$$

High effort is chosen when $\Pi_H - \Pi_L \geq 90$ (+1 pts)

So, we have following cases:

i. If $\Pi_H - \Pi_L < 90$; Costs=0. (+3 pts)

ii. If $90 < \Pi_H - \Pi_L < 340$; Costs = $0,1 * \Pi_H - 0,1 * \Pi_L - 9$ (+3 pts)

iii. If $\Pi_H - \Pi_L \geq 340$; Costs=25 (+3 pts)

4. $3+2=5$ (+10 pts)