


Kosmas Marinakis, Ph.D.

## Lecture 13

Game Theory – part II



**microeconomics II**

first module

### Notes

- ★ Last **homework** available soon
- ★ Not yet available info for the **exam**
- ★ Don't miss **Friday's lecture**

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Static games

### BMW vs. Benz: product choice problem

- ★ **BMW** and **Mercedes** each wish to introduce a **new type** of vehicle in the market
  - ◆ Either a Compact Utility Vehicle (CUV) or
  - ◆ A Compact Cabriolet (Cabrio)
- ★ Firms will be better off if they introduce a **different type** of vehicle
  - ◆ Because the demands in those markets are still small and **cannot accommodate** two competing sellers
  - ◆ Plus firms need to sell a high quantity to **reach their MES**
- ★ Decisions are **non – cooperative**

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Static games    BMW vs. Benz

### Product choice problem

		Mercedes	
		CUV	Cabrio
BMW	CUV	-6, -6	12, 10
	Cabrio	10, 12	-5, -5

- ★ If BMW **hears** that Mercedes is introducing a CUV, its best action is to produce a Cabrio
- ★ Bottom left corner is **Nash equilibrium**
- ★ What is other Nash Equilibrium?  $\_ \_$

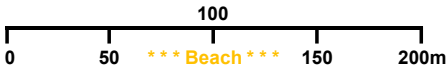
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Static games

### Beach location game

- ★ Imagine a **beach** 200 meters wide
  - ◆ Sunbathers are spread **evenly** along the beach
  - ◆ Two **vendors**, A and B, selling soft drinks
  - ◆ Both charge the **same price**
  - ◆ Customer will buy from the **closest vendor**
- ★ **Where** will the competitors locate?
- ★ Similar to groups of night clubs, car dealerships, etc.  $\_$

~ ~ ~ Sea ~ ~ ~



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Static games

### Another scenario

- ★ Two companies compete in the **smartphone** market
- ★ They need to decide if they will **drop the analog** 3.5mm connector for a digital connector
- ★ New connector does have **advantages** but also creates **disutility** to users
  - ◆ Wired headphones cannot be used as easily
  - ◆ Charging and listening is not possible
- ★ Apple has **more to gain** by the change than Samsung
  - ◆ Samsung has the technology for its phones to be lighter, thinner and waterproof with the old jack, too  $\_$

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Static games Apple vs. Samsung

## Payoffs

		Samsung	
		Analog (3.5mm)	Digital (micro USB)
Apple	Analog (3.5mm)	0, 0	9, 2
	Digital (lightning)	-1, 9	10, 10

★ Observations

- ◆ **Dominant strategy** for Samsung is 'Digital'
- ◆ **Apple** should expect Samsung to go 'digital' soon – so it goes 'digital'
- ◆ **Nash equilibrium**: (Digital, Digital)
- ◆ This **assumes** that Samsung's CEO has **the same view** for the game and is rational.

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Static games

## What is the NE in this game?

		Zhanna	
		Left	Right
Alix	Up	0, 0	1, 1
	Down	1,000,000, 1,000,000	0, 0

★ What is the **outcome** in this game?

★ Outcome (Down, Left) is a **Focal Point**.

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Static games

## Rock – Scissors – Paper

		Player B		
		Rock	Scissors	Paper
Player A	Rock	0, 0	1, -1	-1, 1
	Scissors	-1, 1	0, 0	1, -1
	Paper	1, -1	-1, 1	0, 0

★ There is **no NE** in pure strategies  
no combination of strategies that some player does not want to **deviate unilaterally** from

★ Then, what is the **best strategy (equilibrium)** for this game?

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Static games Mixed strategies

## Mixed strategies

★ Sometimes the best strategy is **not a pure strategy**

★ Players have to do **randomization**  
assign a probability to each strategy and then choose the strategy **randomly** based on assigned probabilities

★ Randomization results to a **mixed strategy**  
player makes a **random choice** from strategy set based on the optimal combination of probabilities.

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Static games Mixed strategies

## Mixed strategies NE in R-S-P

- ★ In the R-S-P game the **NE is in mixed strategies**  
randomize (or mix) all strategies with probability 1/3
- ★ **At the NE**, both players will be doing **the best** they can **given** what their opponent is doing
- ★ If you play any other strategy or mixture, your rival may realize it and **play accordingly to take advantage** of you
- ★ What happens if you play 1/2 Rock and 1/2 Scissors?  
your opponent will **keep playing Rock** and you will never win!

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Static games Mixed strategies

## Some useful facts

1. John Nash proved that **every static game** has **at least one** NE either in pure or in mixed strategies
2. A game might have **both pure and mixed** strategy NE
3. The calculation of the optimal probabilities for the randomization in a mixed strategy NE involves **optimal response functions**
4. Mixed strategies are usual for games like **poker** but **real firms** might **not find it reasonable** to use mixed strategies.

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## Repeated games

- ★ Consider a **static game** which is **repeated** again and again
- ★ **Oligopolistic firms** often play a repeated game they compete for **more than one periods**
- ★ When games are repeated, **two important things** may happen:
  1. Players have a chance for **retaliation**
  2. Players can develop **reputations**

## Sustainability of non-Nash outcomes

- ★ The firms can decide to **collude** implement an outcome **better than the NE** (but **not a NE**)
- ★ Collusion is **not stable** players have an **incentive to deviate** (cheat)
- ★ If a player decides to cheat, he can get away with a higher profit **for that period**
- ★ BUT, starting **from the next period**, the player who was cheated upon will retaliate by choosing his NE strategy

## Pricing problem

		PlayStation	
		Low price	High price
Xbox	Low price	10, 10	100, -50
	High price	-50, 100	50, 50

- ★ NE implies that they **both set low prices**
- ★ Collusion is **better** than NE but there is **incentive** for **cheating** it is **even better** for a firm to set a low price while the other firm sets a high price
- ★ Collusion **may be sustained** if the game is repeated firms might adopt a **tit-for-tat strategy**

## Tit-for-Tat strategy

- ★ Retaliation is often called **tit-for-tat** strategy *I trust you and play the collusive strategy but if you cheat, I will be playing my Nash strategy forever*
- ★ The tit-for-tat strategy is a **trigger strategy** everyone trusts everyone else **until** someone... pushes the trigger
- ★ Once the **trigger is pushed**
  - ◆ The **cheater** loses from **next period** (collusion → NE)
  - ◆ The **fair player** loses too but **does not trust** the cheater anymore
  - ◆ For the **fair player** the NE is better than to be **cheated upon**

## Indefinite repetition

- ★ What if the game is **infinitely repeated**?
- ★ Competitors repeatedly set price **every period**, forever
- ★ **Tit-for-tat** strategy makes sense
- ★ If a player **cheats**:
  - ◆ The **other player** will be playing the **Nash strategy**, forever
  - ◆ The **cheater** will get high profits **for that period** but from the **next one** will be getting much less
- ★ The threat of retaliation is **credible**

## Finite repetition

- ★ What if the game is repeated a **known finite number** of times?
- ★ Lets take things **from the end**
  - ◆ In the **last period** there is **no possibility of retaliation**, thus, everyone will cheat
  - ◆ Yes, but if everyone cheats in the last period, there is **no fear of retaliation** to the **second to last period**
  - ◆ So, there is **no possibility of retaliation** for **any period**
- ★ The **threat** of retaliation is **not credible** collusion is **not sustainable**

Repeated games

## Cooperation in repeated games

- ★ Cooperation is **at best difficult**
  - ◆ **Conditions may change** in the long-run
  - ◆ Need a **small number** of firms
  - ◆ Need **stable demand** and **cost** conditions
- ★ Sometimes, a firm might have a **legitimate reason** to lower price and avoid to do it  
 fear that such action may be **misunderstood** and push **accidentally** the trigger. ↘

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Dynamic games

## Sequential games

- ★ In sequential games players **move in turns**, responding to each other's actions and reactions
  - ◆ Ex: **Stackelberg** model
  - ◆ Responding to a competitor's **ad campaign**
  - ◆ **Entry** decisions. ↘

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Dynamic games    BMW vs. Benz

## BMW vs. Benz – revisited

		Mercedes	
		CUV	Cabrio
BMW	CUV	-6, -6	12, 10
	Cabrio	10, 12	-5, -5

- ★ If both firms announce their decisions **independently** and **simultaneously**, they may **both lose money**
- ★ What if Mercedes **sped up** production and introduced a new model **first**?
  - ◆ Now there is a **sequential game**
  - ◆ BMW will have to **produce the opposite** of what Mercedes produced. ↘

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Dynamic games    BMW vs. Benz

## Extensive form

		Mercedes	
		CUV	Cabrio
BMW	CUV	-6, -6	12, 10
	Cabrio	10, 12	-5, -5

- ★ The above bi-matrix **does not depict** the game with clarity anymore
- ★ We have to represent possible moves in the **extensive form** of a **decision tree**  
 we can **work backward** from the best outcome for BMW. ↘

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Dynamic games    BMW vs. Benz

## Decision tree

		Mercedes	
		CUV	Cabrio
BMW	CUV	-6, -6	12, 10
	Cabrio	10, 12	-5, -5

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Dynamic games

## Sub-game Perfect NE

- ★ In the previous product-choice game we **split** the game into sub-games
- ★ Then we found the NE in **every** sub-game
- ★ **Sub-game Perfect NE** (SPNE): A combination of strategies which is a NE in **every subsequent sub-game** that includes this combination
- ★ We will use the SPNE as the **basic equilibrium notion** in dynamic games. ↘

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## The first-mover advantage

- ★ In the previous product-choice game, there is a clear **advantage to moving first**
- ★ In **quantity competing oligopoly** there is the **same** advantage
  - ◆ The firm which goes first can choose a **large level of output**, thereby **forcing the second firm** to choose a small level
  - ◆ **Compare** Cournot vs. Stackelberg.

Thank you!



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